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The Maximum Likelihood Reconstruction Method for JET Neutron Tomography

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ABSTRACT

The JET neutron profile monitor ensures coverage of the neutron emissive region that enables tomographic reconstruction. However, due to the availability of only two projection angles and to the coarse sampling, tomography is a limited data set problem. A reconstruction method based on the maximum likelihood principle is developed for solving the reconstruction problem. A smoothing operator, defined as median filtering which uses a sliding window moving along magnetic contour lines, is used to compensate for the lack of experimental information. The method is tested on numerically simulated phantoms with shapes characteristic for this kind of tomography. Significant reconstructions of experimental data are reported.

1. INTRODUCTION

The JET neutron profile monitor is a unique instrument among neutron diagnostics available at large fusion research facilities [1-3]. The profile monitor comprises two fan shaped multi-collimator cameras, with 10 channels in the horizontal camera and 9 channels in the vertical camera. A schematic drawing of the JET neutron emission profile monitor, showing the 19 lines of sight is presented in Fig.1. Each line of sight is equipped with a set of three different detectors:

- a NE213 liquid organic scintillator with Pulse Shape Discrimination (PSD) electronics for simultaneous measurements of the 2.5MeV D-D neutrons, 14MeV D-T neutrons and γ-rays,
- ii) a BC418 plastic scintillator, insensitive to γ -rays with $E\gamma < 10$ MeV for the measurements of 14MeV D-T neutrons and
- iii) a CsI(Tl) scintillation detector for measuring the hard X-rays and gamma emission in the range between 0.2 and 6MeV. The collimation can be adjusted by use of two pairs of rotatable steel cylinders. The size of the collimation can modify the count rates in the detectors by a factor of 20 [4]. The instrument has a time resolution currently of 10ms.

The plasma coverage can be used for neutron or γ -ray tomography but the texistence of only two views (projections in tomographic terms) and the coarse sampling in each projection leads to a highly limited data set tomographic problem. A number of valuable approaches have been developed for tomographic reconstruction of the two-dimensional 2-D neutron and gamma emissivity.

A Hybrid Pixel/Analytic Algorithm (HPAA), which involves a poloidal Fourier analysis and a radial Abel inversion, starting from outside and working inward is reported in Ref.5. During a series of experiments with tritium in deuterium plasmas in JET, the temporal evolution and the two dimensional (2-D) spatial profiles of the 2.5 and 14MeV neutron emissivities from D-D and D-T fusion reactions were inferred from measurements with the JET neutron emission profile monitor [5-6].

Ingesson [7] applied a Constrained Optimization Method (ICOM). This method was widely used earlier for tomographic reconstructions to soft X-ray and bolometer measurements at JET. It uses anisotropic smoothness on flux surfaces as objective function (a priori physical information about the expected emission profile) and measurements as constraints. Thus, the method searches for the emissivity distribution that is constant on flux surfaces and gently varying in the radial direction. Instead of traditional square pixels, a grid of pyramid local basis functions are used for the discretization of the tomographic problem [8]. ICOM was extensively used for the diagnosis of fast ions in the JET tokamak and relevant results were reported for γ -ray [9-11] and neutron [12-15]†tomographic emissivity reconstruction.

The Minimum Fisher Regularization (MFR), was applied to the tomographic reconstruction of both soft X-ray and bolometric data [16-17]. In principle, the Fisher information of the unknown 2-D distribution is minimized, while the measurements are taken into account as constraints, using Lagrangian multipliers. Instead of treating the fully nonlinear problem, Anton et al. [16] exploited only the central idea and achieved a minimization of the Fisher information of the unknown 2-D distribution by several linear regularization steps. The method was used for the neutron emissivity reconstruction and 2-D spatial distributions of D-D and D-T neutron emission in JET ELMy H-mode plasmas with Tritium puff were reported [18-19].

The aim of this paper is to prove that the Maximum Likelihood (ML) reconstruction method, which has been proven to work with limited data set problems [20-21], can be customized and successfully used for JET neutron tomography, in order to provide both accurate and fast reconstructions. The method is evaluated both on phantoms (numerically simulated distributions) and on experimental data.

2. IMPLEMENTATION OF THE MAXIMUM LIKELIHOOD METHOD

In 2-D tomography systems, measurements are taken along lines of sight, and can essentially be represented by line integrals; i.e. the measurement *p* is given by straight line integrals of the emissivity f(x, y), where *x* and *y* are Cartesian coordinates of the plane. The emissivity function can be appropriately discretized on a 2-D grid. For this purpose, the reconstruction area is divided into pixels that are sufficiently small for emissivity variations within a pixel to be negligible. The contribution matrix element W_{ik} represents the proportion of the emission f_i from pixel *i* accumulated in detector *k* (the weighting matrix). The basic set of tomographic equations is:

$$p_{k} = \sum_{i=1}^{N_{p}} w_{ik} \cdot f_{i}, \quad k = 1, 2, ..., N_{d}$$
(1)

where N_p and N_d are the numbers of pixels and detectors, respectively. This set of linear equations represents the linear inverse problem. It is evident that, even with exact data constraints, this inversion cannot be uniquely performed when there are fewer data than pixels, as is generally the case in plasma tomography.

2.1 MAXIMUM LIKELIHOOD

The ML method arose in clinical application as a promising reconstruction method with the potential

to yield higher resolution and lower noise reconstructions than conventional methods (see e.g Refs. 22-23). It can be derived based on the principles of the Bayesian tomography. Let *P* represent a set of measured projection data, and let *F* represent a model of the object under consideration. The goal is to assign values to *F* that accurately reflect the objects being inspected from the noisy and potentially incomplete data, *P*. In ML estimation, the estimated model F_{ML} is taken to be the value of *F* which maximizes the likelihood, L(P|F), of observing *P*, assuming that *F* is correct. Equivalently, and more commonly, the log-likelihood can be maximized.

More precisely, in ML tomography, it is assumed that the emission is a Poisson process and p_k is a sample from a Poisson distribution whose expected value is:

$$\sum_{k} w_{ik} f_i \tag{2}$$

Then the probability of obtaining the measurement $P = \{p_k | k = 1,...N_d\}$ if the image is $F = \{f_i | i = 1,...N_p\}$ (the so-called likelihood function) is:

$$L(P/F) = \prod_{k} \left[\frac{1}{p_{k'}} \left(\sum_{i} w_{ik} f_{i} \right)^{p_{k}} \times exp\left(-\sum_{i} w_{ik} f_{i} \right) \right]$$
(3)

The ML method solves the problem of evaluating F, if P is known, by selecting the particular F which maximizes L(P|F). This is a difficult nonlinear optimization problem and until the application of the iterative Expectation Maximization (EM) algorithm by Shepp and Vardi [24] there was no method with known convergence properties for generating the ML solution. The iterative solution is given by the following formula:

$$f_i^{(iter+1)} = f_i^{(iter)} \frac{\sum_k^{k} w_{ik}}{\sum_l^{l} w_{jl} f_j^{(iter)}}}{\sum_k^{k} w_{ik}}$$
(4)

where $f_i^{(iter)}$ is the reconstructed image for the iteration *iter*, *i* and *j* are image element indices, *k* and *l* are projection element indices. Due to the imbricated sums in Eq. 4 the algorithm is computationally demanding. This leads to long reconstruction times that are not acceptable for routine clinical application. In consequence the applicability of the method in the medical field is limited. However, for a limited data set problem, the amount of computation for solving the iterative problem is not so time-consuming and successful results were reported for several applications. (see e.g. Refs. 25-28).

A well known characteristic of the ML algorithm is that the unconstrained maximum-likelihood estimator has a fundamental noise artifact that worsens as the iterative algorithm climbs the likelihood hill. Even the likelihood function is monotonically increasing with the iteration number, the best reconstruction is obtained before irregular high amplitude patterns or global distortions arise. In consequence, a criterion for optimal stopping of the algorithm must be introduced. We found that the correlation coefficient between reconstructions obtained at successive iterations reaches its maximum value for the best reconstruction. The correlation coefficient is given by the following equation:

$$corr = \frac{N^2 \sum_{i} f_i^{iter} f_i^{iter-1} - \sum_{i,j} f_i^{iter} \sum_{i} f_i^{iter-1}}{\left[N^2 \sum_{i} \left(f_i^{iter}\right)^2 - \left(\sum_{i} f_i^{iter}\right)^2\right]^{\frac{1}{2}} \left[N^2 \sum_{i} \left(f_i^{iter-1}\right)^2 - \left(\sum_{i} f_i^{iter-1}\right)^2\right]^{\frac{1}{2}}}$$
(5)

where f_i^{iter-1} represents the reconstructed image at the previous iteration and f_i^{iter} at the current iteration.

2.2 THE GEOMETRY OF JET NEUTRON TOMOGRAPHY

From the tomographic point of view, the major problem is that the JET neutron profile monitor system has only two fairly coarse views of the plasma. Dividing the reconstruction space in 20×35 pixels (pixel size of 90×90mm) it means that an image with 700 pixel values must be retrieved from 19 experimental data. The scarcity of the data is illustrated also by the weighting matrix, represented as an image (Fig. 2 - left); even after taking into account the beam width (Fig. 3), the non-uniformity of the domain coverage by the lines of sight persists (Fig.2 - right).

Moreover, according to the Nyquist theorem, the number of resolvable harmonic constituents of the 2-D profile is lower than the number of lines of sight. Therefore, the tomographic reconstructions will only show general features of the emission profile. Information is simply not available to obtain improved results unless *a priori* knowledge about the emission profiles is taken into account.

2.3 SMOOTHING

Smoothing can be introduced in order to compensate for the lack of experimental information. Different approaches were developed and reported in fusion studies. If a regularization method is used, smoothness can be introduced in the expression of the objective function. The general functional used to quantify the global unsmoothness of the solution can be formulated by a scalar product (see Ref. 7, Appendix C):

$$\langle f | \Omega | f \rangle = \sum_{i} \left\{ a_0 f_i^2 + \left[a_x \left(\frac{\partial f}{\partial x} \right)^2 + a_y \left(\frac{\partial f}{\partial y} \right)^2 \right]_i + \left[a_{xx} \left(\frac{\partial^2 f}{\partial x^2} \right)^2 + a_{xy} \left(\frac{\partial^2 f}{\partial x \partial y} \right)^2 + a_{xx} \left(\frac{\partial^2 f}{\partial y^2} \right)^2 \right]_i \right\}$$
(6)

where *W* is the unsmoothness operator. The a_0 term penalizes large values of f(x, y). The first derivative terms force the solution to be as flat as possible, whereas the second derivative terms force it to be as smooth as possible. MFR, a kind of Phillips-Tikhonov regularization, uses the first derivative terms. ICOM uses an expression which contains both first and second derivative terms. The expression is derived based on the assumption that emission in a tokamak is approximately a flux function: the discrepancy is smaller than 10% [29] for soft X-ray emissions, for which ICOM was initially developed. Therefore, an anisotropic diffusion-like smoothness function is introduced [30]. It takes into account that the emission profile is smoother in the poloidal direction than in the radial one.

A different approach is suggested by Ertl [31], based on the preblur concept [32]. It starts from the assumption that the object of interest contains correlations, typically between neighbouring pixels. In consequence, the image f is expressed as a blurred version of an underlying hidden image h, which itself is uncorrelated:

$$f_i = \sum_i c_{ji} h_j \tag{7}$$

where c_{ji} is the matrix that defines the actual correlation. Preblur is not an *a posteriori* smoothing of the reconstruction, because the formalism is applied to the hidden image *h*, whereas the objective function of the tomographic problem is calculated for the visible result *f*; Meantime *f* has to be fully compatible with the data constraints. Ertl [31] use Gaussian correlation of neighbouring pixels.

In the present approach we also assume smoothness on flux surfaces. We implemented the smoothing operator as one-dimensional median filtering, using a sliding window which moves on the magnetic contour lines:

$$f_i = \sum_{\substack{j = -w_{med} \\ w_{med} \in L_k}} m_{ji} h_j$$
(8)

where m_{ji} is the matrix which defines the window-based median filter, w_{med} is half of the width of filtering window and L_k designates a close magnetic contour line L_k . The iterative ML algorithm (Eq. 4) works directly on the reconstructed image which is successively updated. This allows image manipulation at each iteration for introducing *a priori* knowledge. Therefore median filtering is applied, as described, at each iteration. In order to obtain additional smoothing, we transformed the experimental projection by resampling, using spline interpolation (Fig.4). Projection resampling implies the introducing of virtual lines of sight (Fig.5) which ensures an improved coverage of the reconstruction domain. By numerical simulations, we found that the effect of these smoothing techniques are stronger enough to make useless the implementation of beam-width.

3. RESULTS AND DISCUSSIONS

The ML method was implemented as described previously. Resampling was performed so that the size of the synthesized signals is $n_{res} = 4$ times the initial one. This value proved to be optimal for obtaining both appropriate smoothing and fast enough calculation time: resampling implies an increase of the number of projection elements p_k and the corresponding resize of the weighting matrix W_{ik} . The width of the median filtering w_{med} was set at 1/10 of the size of the vector describing the magnetic contour line. As the reconstruction geometry is fixed, the weighting matrix was precalculated in order to reduce computing time. ML is not significantly sensitive to a specific initial specification, so, for simplicity, a constant initial solution was used in the iterative algorithm.

The method was tested on various phantoms with shapes characteristic for this kind of tomography and representative results are presented here (Figs.6-10). The phantom in Fig.6 is described by the relation:

$$ph(r) = \begin{cases} \left(x^2 + y^2\right)^{3/2}, \text{ for } \left(x^2 + y^2\right)^{1/2} < \frac{N_{px}}{2} \\ \left[1 - \left(x^2 + y^2\right)^{1/2}\right], \text{ for } \frac{N_{px}}{2} < \left(x^2 + y^2\right)^{1/2} < N_{px} \end{cases}$$
(9)

where N_{px} is the number of pixels on the horizontal dimension of the reconstruction grid. Phantoms in Figs. 7-8 were derived from the same circular symmetrical shape, by cutting half of the shape. Virtual magnetic contour lines were simulated by circles placed concentrically on the reconstruction grid. For the phantom in Fig. 9 the half-hollow shape from Fig.7 was distorted to a elliptical symmetrical one (the vertical semi-axis is twice the horizontal one) and a centred

Gaussian
$$A \cdot exp\left(-\frac{x^2}{2\pi\sigma_x^2} - \frac{y^2}{2\pi\sigma_y^2}\right)$$
 was superimposed ($\sigma_x = 0.8$ and $\sigma_x = 1.6$ and $A = 0.18$. Virtual magnetic contour lines were simulated by concentric ellipses for which the ratio between the vertical

semi-axis and the horizontal one is equal to 2.

Good reconstructions are obtained for the "hollow" and "banana" phantoms (Figs.6-7). A more difficult case is the reconstruction of the "banana" phantom, rotated by 180 degrees about the vertical axis (Fig. 8). The diverging chords fan spread wider in this region and this results in a reduced information density leading to a shadow effect. There are more possibilities in this region to distribute each detector signal among different cells than in the region close to the detectors and this may result in reduced spatial resolution. However, the decline in reliability with increasing distance from the detector proved to be a tolerable effect. The shape of the "banana" is reconstructed without global distortions. A blurring effect is superimposed on the image, however this does not alter significantly the spatial resolution. We appreciate that this is also the inherent effect of smoothing which is, on the other hand, essential for obtaining correct reconstructions. The spatial resolution of the method is sufficient to resolve the complex shapes like "banana" plus peak (Fig.9).

The method was applied for the analysis of experimental data recorded at JET and significant results are reported (Figs.10-13). In order to evaluate the performances of the ML method a comparison with the results provided by the ICOM method [33] was performed. Similar reconstruction of a "peak" phantom (most frequent distribution shape) is obtained by both methods (Fig.10). This is the reconstructions of the DT-neutron emissivity profile in the experiment with the T-puff in the deuterium plasma at 22.5s during the D neutral beam injection. In such experiments, tritium is injected in 'trace' amount (typically $n_I / (n_T + n_D) < 3\%$ and the temporal evolution of the tritium spatial distribution can be detected by observation of the 14MeV neutron emission, allowing non-perturbative transients experiments. The neutron profile is a typical one for plasma with tritium which has penetrated to the plasma core in full. The reconstruction of a "banana" distribution is presented in Fig. 11. In this case DT-neutron emission was measured in the ohmic deuterium discharge during the off-axis injection of the T neutral beam. Comparable reconstructions are obtained by both methods. In comparison with ICOM, the ML reconstruction is affected by a slightly vertical

asymmetry. The reconstruction of a combined "peak" plus "banana" distribution is illustrated in Fig.12. This profile was recorded just after the T-puff in the same discharge as it has been presented in the Fig.10, and tritons partly penetrated to the plasma core from the periphery. Thinner shapes are obtained in case of ML method. We appreciate that this difference is due to the difference in the definition of the smoothing: ICOM uses smoothing in both poloidal and radial direction (anisotropically) while ML implements smoothing only along magnetic contour lines.

Besides spatial information, tomography is able to provide also information about the temporal evolution of the neutron emissivity. The capability of the ML method to reveal this kind of information is illustrated in Fig.13, where six reconstructions are taken in the temporal interval 20.87-21.32s. They show the temporal evolution of the D-T 14MeV neutron emissivity in a trace tritium experiment. The tomographic reconstruction demonstrates a relaxation of the high density plasma, which is heated by D neutral beams after the T-puff at 20.5s. An evolution of the tritium penetration from the edge toward the core can be clearly seen.

MATLAB was used as a suitable environment for developing and testing the method. In this implementation the time needed for a reconstruction is lower than 3.5 minutes since 15-20 iterations are typically enough to reach the maximum value of the correlation coefficient (Eq. 5). This is two time faster than a single run of ICOM, which needs multiple runs for data preparation. As the iterative algorithm (Eq. 4) can not be formulated in a matricial form (most suitable for MATLAB), we expect to obtain a significant improvement of the calculation time in a further optimized implementation. The computation speed, combined with accurate reconstruction represents an advantage of the ML method which will qualify it as an appropriate method for inter-shot analysis.

CONCLUSION

In conclusion we appreciate that the ML reconstruction method provides good reconstructions in terms of shapes and resolution. The smoothing techniques, introduced in order to compensate for the lack of experimental information, induce a blurring effect but the correct reconstructions are still practicable. The strategy used for smoothing implementation allows fast reconstructions. The possibility of further optimization qualifies ML as a candidate for inter-shot analysis.

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Figure 1: Schematic view of the JET neutron emission profile monitor showing the lines of sight.



Figure 2: The reconstruction domain coverage (the weight matrix represented as an image): in case of infinitely thin line of sights (left) and taking into account the beam



Figure 3: Beam width representation



Figure 4. Projection resampling exemplified.



Figure 5: Reconstruction of the hollow phantom.



Figure 6: Reconstruction of the "banana" phantom.



Figure 7: Reconstruction of the symmetrically reversed "banana" phantom.



Figure 8: Reconstruction of the "banana" plus peak phantom



Figure 9: Neutron emissivity reconstruction for Pulse No: 61132 at 22.92 s: ICOM (left) and ML (right).





Figure 10: Neutron emissivity reconstruction for Pulse No: 61237 at 6.22 – 6.27s s: ICOM (left) and ML (right)

Figure 11. Neutron emissivity reconstruction for shot 61132 at 2.67s: ICOM (left) and ML (right).



Figure 12. Temporal evolution of the neutron emissivity for Pulse No: 61141 (from 20.87 s to 21.32s)

