

---

EFDA–JET–CP(04)01-13

H Meister, R Fischer, C. Giroud, L D Horton, C F Maggi, D Nishijima,  
K-D Zastrow, B Zaniol, ASDEX Upgrade Team  
and JET-EFDA Contributors

# $Z_{\text{eff}}$ from Spectroscopic Bremsstrahlung Measurements at ASDEX Upgrade and JET



# $Z_{\text{eff}}$ from Spectroscopic Bremsstrahlung Measurements at ASDEX Upgrade and JET

H Meister<sup>1</sup>, R Fischer<sup>1</sup>, C. Giroud<sup>2</sup>, L D Horton<sup>1</sup>, C F Maggi<sup>1</sup>, D Nishijima<sup>1</sup>,  
K-D Zastrow<sup>2</sup>, B Zaniol<sup>3</sup>, ASDEX Upgrade Team<sup>1</sup>  
and JET-EFDA Contributors\*

<sup>1</sup>*Max-Planck-Institute for Plasma Physics, EURATOM Association,  
Boltzmannstr. 2, D-85748 Garching, Germany*

<sup>2</sup>*Association EURATOM-UKAEA Fusion, Culham Science Centre, Abingdon, OX14 3DB, UK*

<sup>3</sup>*Consorzio RFX, Associazione EURATOM-ENEA, Corso Stati Uniti 4, I-35127, Padova (Italy)*

\* See annex of J. Pamela et al, "Overview of Recent JET Results and Future Perspectives",  
*Fusion Energy 2000 (Proc. 18<sup>th</sup> Int. Conf. Sorrento, 2000), IAEA, Vienna (2001).*

Preprint of Paper to be submitted for publication in Proceedings of the  
15th HTPD Conference,  
(San Diego, California, USA. 18-22 April 2004)

“This document is intended for publication in the open literature. It is made available on the understanding that it may not be further circulated and extracts or references may not be published prior to publication of the original when applicable, or without the consent of the Publications Officer, EFDA, Culham Science Centre, Abingdon, Oxon, OX14 3DB, UK.”

“Enquiries about Copyright and reproduction should be addressed to the Publications Officer, EFDA, Culham Science Centre, Abingdon, Oxon, OX14 3DB, UK.”

## ABSTRACT.

The effective ionic charge  $Z_{\text{eff}}$  is a means to assess the impurity content of a fusion plasma. It can be derived from measurements of bremsstrahlung intensity. These have been extended at ASDEX Upgrade by the usage of the sight lines for the charge exchange recombination diagnostic. Together with a previously installed sight line array it is now possible to routinely determine the bremsstrahlung intensity over the whole minor radius purely from spectroscopic measurements. In a tokamak where the plasma facing components are made up of various materials, this is necessary to check if measurements are disturbed by line radiation. The bremsstrahlung background of the respective spectra is determined using Bayesian probability theory, giving consistent and improved error statistics. Using the information for electron temperature and density profiles, the  $Z_{\text{eff}}$  profile is determined by an integrated method. The same approach to assess the  $Z_{\text{eff}}$  profile has been demonstrated to be successful also at the JET tokamak.

## 1. INTRODUCTION

A commonly used quantity in nuclear fusion research characterising the global impurity content is the effective charge state  $Z_{\text{eff}} = \frac{\sum_i^n i Z_i^2}{\sum_i^n i Z_i}$ . One method to determine  $Z_{\text{eff}}$  profiles is to measure the bremsstrahlung of the plasma and to calculate  $Z_{\text{eff}}$  using independent measurements of electron density  $n_e$  and temperature  $T_e$ . This approach is used at the tokamak ASDEX Upgrade.

Usually, the measurement of bremsstrahlung is carried out by recording the plasma emission in a certain wavelength range free of line radiation using interference filters and varying types of diodes as detectors. Mostly, a narrow band in the green range of the spectrum is used. The range of up to 5nm around 537nm is reported to be line free in several machines (e.g. Ref. 1-3) whereas JET uses a narrow line-free band around 523nm [4]. At ASDEX Upgrade, the existing filter/detector combinations of the Thomson scattering diagnostic[5] were mainly used for bremsstrahlung measurements, as was previously done at ASDEX[6] and repeated on Frascati Tokamak Upgrade[7]. Although the sensitive Avalanche-diodes used as detectors are very well suited to measure the low intensities of the bremsstrahlung, the interference filters are not optimised for this task. They observe rather broad spectral ranges (up to 80nm) in the near infrared region. Therefore, the bremsstrahlung signals may be disturbed by line radiation and/or thermal radiation from hot parts of the plasma facing components. To compensate for these disadvantages, the procedure of an integrated method[8], has been extended to incorporate the bremsstrahlung emission measured by the charge exchange recombination spectroscopy (CXRS) diagnostic. Together with a previously installed diagnostic it is now possible to determine the bremsstrahlung emission over the whole minor radius purely from spectrally resolved measurements using spectrometers and CCD cameras. In Sec. II an overview is given of diagnostic set-ups at ASDEX Upgrade measuring spectrally resolved bremsstrahlung. Sec. III discusses the principle of determining the bremsstrahlung background in these spectra and using this information to deduce  $Z_{\text{eff}}$  profiles. Sec. IV finally shows an example from JET which demonstrates that this approach to assess  $Z_{\text{eff}}$  profiles is successful at the JET tokamak, as well

## 2. EXPERIMENTAL SET-UP

The measurements of bremsstrahlung intensity at ASDEX Upgrade have been extended by the usage of the sight lines for the CXRS diagnostic[9]. Together with a previously installed sight line array (diagnostic ZEB) it is now possible to routinely determine the bremsstrahlung intensity over the whole minor radius purely from spectroscopic measurements. The sight lines of these diagnostics are shown in Fig.1, mapped onto a toroidal cross-section.

The 12 sight lines of the diagnostic ZEB view the plasma edge at the outer mid-plane. Focusing the light with a convex mirror onto fibre-guides gives a spatial resolution of 1cm. The plasma emission is detected using a Czerny-Turner type spectrograph ( $f = 0.3\text{m}$ ) and a 2D back-illuminated frametransfer CCD-camera (1024×1024 pixel). The spectrograph is equipped with two ruled gratings of 1200 rules per mm, blazed at 300nm and 750nm respectively in order to cover the complete wavelength range from 300nm to 1100nm. In the visible the observed wavelength range at one grating position is up to 30nm. The minimum cycle time of the camera is mainly determined by the readout time of 45ms for the current set-up. Mostly, a cycle time of 60ms is applied, which is a good trade-off with respect to the signal-to-noise ratio in the wavelength range of 532-562nm which is usually used for  $Z_{\text{eff}}$  determination.

One sight line array of the CXRS diagnostic is used during this work to cover the whole minor radius in the outer mid-plane. The array consists of 12 sight lines which are focused onto fibre-guides and detected by a 2D intensified CCD camera (512×512 pixel) coupled to a 1m Czerny-Turner type spectrograph with a grating with 2400 rules per mm. For charge exchange measurements of ion temperature and toroidal rotation velocity the C-VI charge exchange line at 529.05nm ( $Dn 87$ ) is observed in the wavelength range of 526-532nm.

Both diagnostics are absolutely calibrated. For the intensity calibration we place a calibrated integrating sphere inside the vessel in front of the optics during maintenance periods. Thus all optic components are considered in the same way during calibration as during experimental measurements. In order to further improve the relative channel-to-channel calibration a discharge with a radial sweep of the plasma but otherwise constant parameters is used. The absolute value of the calibration factor is checked during a high-density discharge with known low impurity content.

## 3. DATA ANALYSIS

The spectra measured by the ZEB and CXRS diagnostics normally show one or several spectral lines. Nonetheless there remain always enough regions of the spectra which exhibit line-free bremsstrahlung background of the plasma. In order to capture the defining characteristics of this background, namely that the background is proportional to  $I_{\text{e}}^2$ , a Bayesian mixture model as in Ref.10 is used. An elaborate analysis of the statistical measurement uncertainties allows to separate statistical noise from line emission. This approach provides a natural way to reliably determine the bremsstrahlung emission irrespective of the fraction of line radiation, while including all uncertainties of the measurements. An example for the fit of the bremsstrahlung background to one sight line of diagnostic ZEB is shown in Fig. 2.

The bremsstrahlung emission from several diagnostics at ASDEX Upgrade, including (but not limited to) those measuring spectrally resolved, is inverted to deduce the  $Z_{\text{eff}}$  profile. In the cold plasma edge line radiation and pseudocontinua from molecular bands dominate the bremsstrahlung background. Therefore, the information from the outermost sight lines of diagnostic ZEB, which usually never touch the separatrix, are used to determine the intensity of a radiative mantle[1]. Its subtraction from the measured intensity of the remaining sight lines, weighted with the path-lengths through the edge region and the widths of the observed wavelength ranges, results in improved deconvolution results.

This approach, explained in detail in Ref. 8, is especially useful in a tokamak where the plasma facing components are made up of various materials (mainly C and W in ASDEX Upgrade) in order to check if measurements are disturbed for various reasons, e.g. due to line radiation. Consistent  $Z_{\text{eff}}$  values are derived and the limits of validity for each diagnostic involved are clearly identified. An example for  $Z_{\text{eff}}$  profile deconvolution is shown in the right column of Fig. 3. In this case  $T_e$  and  $n_e$  profiles are taken from the Thomson scattering diagnostic.

In the matrix inversion method used for deconvolving  $Z_{\text{eff}}$  profiles,  $T_e$  and  $n_e$  are assumed to be known exactly when comparing measured and calculated sight line intensities. Hence, the uncertainties of the  $T_e$  and  $n_e$  profiles are not reflected in the confidence band of the resulting  $Z_{\text{eff}}$  profile. The sensitivity of  $Z_{\text{eff}}$  to the uncertainties in these profiles can be estimated by Monte Carlo variation, using the multi-normal distribution inferred from the variance-covariance matrix of a least squares fit to the  $T_e$  and  $n_e$  raw data, using an appropriate regression model (left column of Fig.3: spline fits in black, varied profiles in gray). Significant variation of the resulting  $Z_{\text{eff}}$  profile (gray profiles in lower left graph of Fig.3) is seen mainly towards the plasma edge where the uncertainties in the density profiles are largest and also most important due to steep gradients and the strong dependence of  $Z_{\text{eff}}$  on  $n_e$ . In the plasma centre the uncertainty from  $T_e$  and  $n_e$  variation does not exceed the one from uncertainties in the measurements.

#### 4. EXPERIMENTAL RESULTS FROM JET

At the JET tokamak there is no dedicated diagnostic to determine  $Z_{\text{eff}}$  profiles from bremsstrahlung radiation. At present only one vertical and one horizontal sight line of the array described in Ref. 11 are used to determine a line averaged value from visible bremsstrahlung emission<sup>4</sup>. However, by porting the evaluation procedure used at ASDEX Upgrade it could be demonstrated that the bremsstrahlung emission underlying the spectra of the charge exchange recombination diagnostic at JET may be used to deduce  $Z_{\text{eff}}$  profiles. In this case the intensity of the bremsstrahlung background is not determined by the Bayesian model but taken directly from the background of the fitted charge exchange lines.  $T_e$  and  $n_e$  profiles are calculated by fitting a cubic spline to the data from several diagnostics. In case of  $T_e$  this is the data from electron cyclotron emission and the one from edge LIDAR Thomson scattering. In case of  $n_e$  the spline is fitted to the data of the centre and edge LIDAR Thomson scattering diagnostic. As an example of this approach Fig. 4 shows the spline fits

to the raw data (left column) and the resulting  $Z_{\text{eff}}$  profile (right column). As at ASDEX Upgrade, the main source of uncertainty in the resulting  $Z_{\text{eff}}$  profile is the accuracy of the  $n_e$  profile. Again, for the deconvolution  $n_e$  is assumed to be known exactly and the confidence band of  $Z_{\text{eff}}$  does not reflect this uncertainty.

## ACKNOWLEDGMENTS

The authors would like to thank A. Bacciero for providing the spline fitting routines to  $T_e$  and  $n_e$  data at JET.

## REFERENCES

- [1]. D. G. Whyte, M. R. Wade, D. F. Finkenthal, K. H. Burrell, P. Monier-Garbet, B. W. Rice, D. P. Schissel, W. P. West, and R. D. Wood, Nucl. Fusion **38**, 387 (1997).
- [2]. E. S. Marmor, R. L. Boivin, R. S. Granetz, J. W. Hughes, B. Lipschultz, S. McCool, D. Mossessian, C. S. Pitcher, J. E. Rice, and J. L. Terry, Rev. Sci. Inst. **72**, 940 (2001).
- [3]. F. Orsitto, M. R. Belforte, M. Borra, A. Brusadin, and E. Giovannozzi, Rev. Sci. Inst. **68**, 1024 (1997).
- [4]. H. Weisen, D. Pasini, A. Weller, and A. W. Edwards, Rev. Sci. Inst. **62**, 1531 (1991).
- [5]. H. Murmann, S. Götsch, H. Röhr, H. Salzmann, and K. H. Steuer, Rev. Sci. Inst. **63**, 4941 (1992).
- [6]. H. Röhr, K. H. Steuer, and ASDEX Team, Rev. Sci. Inst. **59**, 1875 (1988).
- [7]. F. Orsitto, M. R. Belforte, A. Brusadin, E. Giovannozzi, D. Pacella, and M. J. May, Rev. Sci. Inst. **70**, 925 (1999).
- [8]. H. Meister, R. Dux, L. D. Horton, B. Kurzan, P. J. McCarthy, H. Zohm, and ASDEX Upgrade Team, Rev. Sci. Inst. **74**, 4625 (2003).
- [9]. C. F. Maggi, L. D. Horton, B. Zaniol, P. Franzen, H. Meister, D. Nishijima, A. Stäbler, and ASDEX Upgrade Team, in Europhysics Conference Abstracts (CD-ROM, Proc. of the 30th EPS Conference on Controlled Fusion and Plasma Physics, St. Petersburg, 2003), edited by R. Koch and S. Lebedev (EPS, Geneva, 2003), vol. **27A**, pp. P-1.63.
- [10]. R. Fischer, K. M. Hanson, V. Dose, and W. von der Linden, Physical Review **E 2**, 1152 (2000).
- [11]. P. D. Morgan, K. H. Behringer, P. G. Carolan, M. J. Forrest, N. J. Peacock, and M. F. Stamp, Rev. Sci. Inst. **56**, 862 (1985).



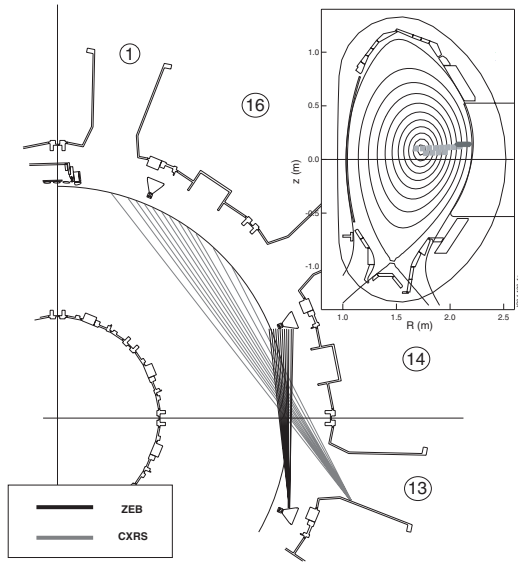


Figure 1: Sight lines measuring bremsstrahlung intensity resolved at ASDEX Upgrade

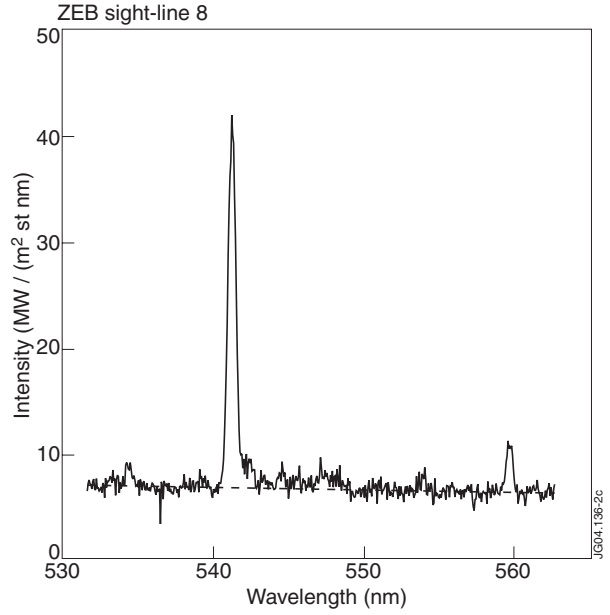


Figure 2: Fit of the bremsstrahlung background (---) to sight line 8 of the ZEB diagnostic in the case of a background plasma with relatively strong spectral lines (Pulse No: 18468,  $t = 3.5$ s)

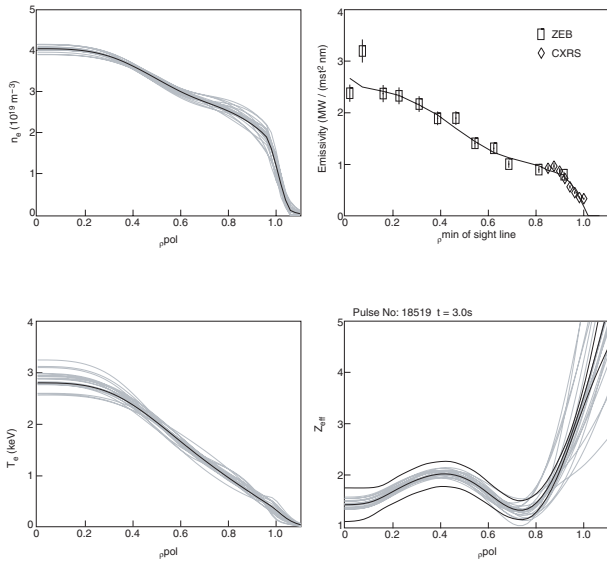


Figure 3: ASDEX Upgrade discharge Pulse No: 18519,  $t = 3.0$ s. Left column:  $n_e$  and  $T_e$  profiles (black line: spline fit to raw data, gray lines: Monte Carlo variation of splines). Right column: emissivity per sight line plotted with  $r_{pol}$  of sight line as x-axis, measured (symbols) and reproduced by deconvolution (-) and  $Z_{eff}$  profile (-) with confidence band (---) corresponding to original spline fits.  $Z_{eff}$  profiles in gray correspond to the respective varied  $T_e$  and  $n_e$  profiles.

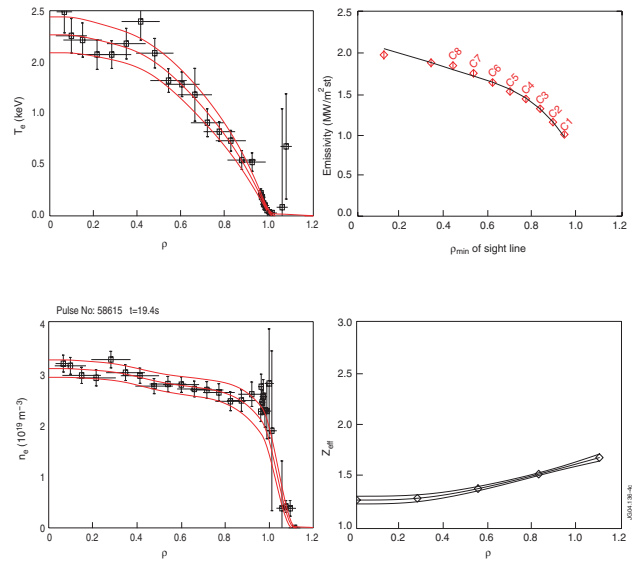


Figure 4:  $T_e$ ,  $n_e$ , bremsstrahlung emission per sight line and  $Z_{eff}$  profiles for JET discharge Pulse No: 58615,  $t = 59.365$